

Ответы к самостоятельной работе ...

- 1) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 10 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 5x^2 - 5y^2 + C, f'(z) = 5z^2 - 5i + C$;
 б) $u(x, y) = 20xy + C, f'(z) = -10iz^2 - 5i + C$
 нет
- 2) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 6 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 3x^2 - 3y^2 + C, f'(z) = 3z^2 - 4i + C$;
 б) $u(x, y) = 12xy + C, f'(z) = -6iz^2 - 4i + C$
 нет
- 3) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 4 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 2x^2 - 2y^2 + C, f'(z) = 2z^2 - 10i + C$;
 б) $u(x, y) = 8xy + C, f'(z) = -4iz^2 - 10i + C$
 нет
- 4) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 9 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 2x^2 - 2y^2 + C, f'(z) = 2z^2 - 3i + C$;
 б) $u(x, y) = 8xy + C, f'(z) = -4iz^2 - 3i + C$
 да
- 5) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 4 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 4x^2 - 4y^2 + C, f'(z) = 4z^2 - 2i + C$;
 б) $u(x, y) = 16xy + C, f'(z) = -8iz^2 - 2i + C$
 нет
- 6) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 3 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = x^2 - y^2 + C, f'(z) = z^2 - 7i + C$;
 б) $u(x, y) = 4xy + C, f'(z) = -2iz^2 - 7i + C$
 нет
- 7) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 2 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 5x^2 - 5y^2 + C, f'(z) = 5z^2 - 7i + C$;
 б) $u(x, y) = 20xy + C, f'(z) = -10iz^2 - 7i + C$
 нет
- 8) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 8 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 4x^2 - 4y^2 + C, f'(z) = 4z^2 - 8i + C$;
 б) $u(x, y) = 16xy + C, f'(z) = -8iz^2 - 8i + C$
 да
- 9) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 1 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 3x^2 - 3y^2 + C, f'(z) = 3z^2 - 8i + C$;
 б) $u(x, y) = 12xy + C, f'(z) = -6iz^2 - 8i + C$
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- 10) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 6 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 3x^2 - 3y^2 + C, f'(z) = 3z^2 - 3i + C$;
 б) $u(x, y) = 12xy + C, f'(z) = -6iz^2 - 3i + C$
 да
- 11) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 8 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 3x^2 - 3y^2 + C, f'(z) = 3z^2 - 10i + C$;
 б) $u(x, y) = 12xy + C, f'(z) = -6iz^2 - 10i + C$
 нет
- 12) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 3 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = x^2 - y^2 + C, f'(z) = z^2 - 6i + C$;
 б) $u(x, y) = 4xy + C, f'(z) = -2iz^2 - 6i + C$
 нет
- 13) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 8 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 4x^2 - 4y^2 + C, f'(z) = 4z^2 - 5i + C$;
 б) $u(x, y) = 16xy + C, f'(z) = -8iz^2 - 5i + C$
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- 14) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 2 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 5x^2 - 5y^2 + C, f'(z) = 5z^2 - 2i + C$;
 б) $u(x, y) = 20xy + C, f'(z) = -10iz^2 - 2i + C$
 нет
- 15) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 10 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 2x^2 - 2y^2 + C, f'(z) = 2z^2 - 9i + C$;
 б) $u(x, y) = 8xy + C, f'(z) = -4iz^2 - 9i + C$
 нет
- 16) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 1 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 3x^2 - 3y^2 + C, f'(z) = 3z^2 - 5i + C$;
 б) $u(x, y) = 12xy + C, f'(z) = -6iz^2 - 5i + C$
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- 17) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 3 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 2x^2 - 2y^2 + C, f'(z) = 2z^2 - 6i + C$;
 б) $u(x, y) = 8xy + C, f'(z) = -4iz^2 - 6i + C$
 нет
- 18) а) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 7 + 2iz, z \in \mathbb{C}$
 а) $u(x, y) = 3x^2 - 3y^2 + C, f'(z) = 3z^2 - 6i + C$;
 б) $u(x, y) = 12xy + C, f'(z) = -6iz^2 - 6i + C$
 нет

- 19) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 4 + 2iz, z \in \mathbb{C}$
 2) a) $u(x, y) = 5x^2 - 5y^2 + C, f'(z) = 5z^2 - 3i + C$; б) $u(x, y) = 20xy + C, f'(z) = -10iz^2 - 3i + C$
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- 20) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 2 + 2iz, z \in \mathbb{C}$
 2) a) $u(x, y) = 4x^2 - 4y^2 + C, f'(z) = 4z^2 - 10i + C$; б) $u(x, y) = 16xy + C, f'(z) = -8iz^2 - 10i + C$
- 21) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 7 + 2iz, z \in \mathbb{C}$
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- 22) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 4 + 2iz, z \in \mathbb{C}$
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- 23) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 10 + 2iz, z \in \mathbb{C}$
 2) a) $u(x, y) = x^2 - y^2 + C, f'(z) = z^2 - 9i + C$; б) $u(x, y) = 4xy + C, f'(z) = -2iz^2 - 9i + C$
- 24) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 10 + 2iz, z \in \mathbb{C}$
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- 25) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 1 + 2iz, z \in \mathbb{C}$
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- 26) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 8 + 2iz, z \in \mathbb{C}$
 2) a) $u(x, y) = x^2 - y^2 + C, f'(z) = z^2 - 3i + C$; б) $u(x, y) = 4xy + C, f'(z) = -2iz^2 - 3i + C$
- 27) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 3 + 2iz, z \in \mathbb{C}$
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- 28) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 1 + 2iz, z \in \mathbb{C}$
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- 29) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 2 + 2iz, z \in \mathbb{C}$
 2) a) $u(x, y) = 5x^2 - 5y^2 + C, f'(z) = 5z^2 - 6i + C$; б) $u(x, y) = 20xy + C, f'(z) = -10iz^2 - 6i + C$
- 30) 1) a) $f'(z) = 1, z \in \mathbb{C}$; б) $f'(z) = 5 + 2iz, z \in \mathbb{C}$
 2) a) $u(x, y) = 4x^2 - 4y^2 + C, f'(z) = 4z^2 - 9i + C$; б) $u(x, y) = 16xy + C, f'(z) = -8iz^2 - 9i + C$